

Quadratic Formula Review

If you just need a numeric approximation to the solution of a quadratic equation, using a programmable calculator to automatically compute and simplify the quadratic formula is convenient. If you don't already have the quadratic formula programmed into your calculator, follow the directions below.

COMMAND	COMMENTS
Press PRGM	<i>Brings up the Program Menu: EXEC EDIT NEW</i>
Arrow over to the NEW menu and choose 1: Create New	<i>Use EDIT to edit an existing program</i>
Type QF (or whatever name you choose) using the ALPHA key and press ENTER*	<i>Names the program QF. Other names are fine too.</i>
:ClrHome	<i>PRGM → I/O menu → 8. Clears the home screen.</i>
:a+bi	<i>MODE → a+bi. Sets the calculator to Complex mode in case you have non-real solutions.</i>
:Prompt A,B,C	<i>PRGM → I/O → 2 for "Prompt". Will prompt the user for A, B and C. You'll always type A, B, and C with the ALPHA key (as well as D, P, and Q later).</i>
:($B^2 - 4AC$) → D	<i>Calculates the discriminant. Use the STO button for the arrow.</i>
:($-B + \sqrt{D}$)/(2A) → P	<i>Calculates the first root</i>
:($-B - \sqrt{D}$)/(2A) → Q	<i>Calculates the second root.</i>
:Disp ROOTS, P ▷ Frac ,Q ▷ Frac	<i>PRGM → I/O → 3 for "Disp". Use ALPHA to type "ROOTS". Use MATH → 1 for "▷ Frac". Displays the two roots (as fractions if applicable).</i>

*Now you're in the program. You'll also need to press ENTER after each line you program.

Example run

We'll use the example equation $2x^2 = 9(x + 2)$.

First we rewrite in standard form: $2x^2 - 9x - 18 = 0$.

Then we identify the coefficients: $A = 2, B = -9, C = -18$.

Now run the program. Use PRGM → EXEC → choose your QF program. Press ENTER.

Type in your $A, B,$ and C values as prompted, pressing ENTER after each.

Your calculator should then output the two solutions, 6 and $-3/2$.

If you press ENTER again immediately, your calculator will run a fresh version of the program (good if you're doing a bunch of quadratic formula problems in a row).

Example run 2

For the equation $x^2 - 2x + 2 = 0$, identify that $A = 1, B = -2, C = 2$

Run the program to obtain the solutions $1 + i$ and $1 - i$.

Use algebra to write the equation in standard form ($ax^2 + bx + c = 0$), and then use your program to solve.

1) $x^2 + x = 42$	2) $x^2 + 10 = 11x$
3) $t^2 + 8 = 4t$	4) $2x(x - 5) = 12$
5) $2x^2 + 3 = 2(x - x^2) + 10$	6) $\frac{5x}{x^2 + 1} = 2$
7) $(x + 3)(3x + 5) = 7$	8) $(x + 3)(x - 2) = 50$
9) $9x^2 = \frac{5(x+1)}{2} + 2x$	10) $x^2 = 4x - 53$
11) $\sqrt{x + 4} = x - 2$	12) $\sqrt{x + 7} = x + 1$
13) $2 + \sqrt{2x - 1} = x$	14) $4 + \sqrt{2x^2 - 8} = 0$
15) $4x(x - 1) + 1 = 0$	

In standard form:

1) $1x^2 + 1x - 42 = 0$	2) $1x^2 - 11x + 10 = 0$
3) $1t^2 - 4t + 8 = 0$	4) $2x^2 - 10x - 12 = 0$
5) $4x^2 - 2x - 7 = 0$	6) $2x^2 - 5x + 2 = 0$
7) $3x^2 + 14x + 8 = 0$	8) $1x^2 + 1x - 56 = 0$
9) $18x^2 - 9x - 5 = 0$	10) $1x^2 - 4x + 53 = 0$
11) $1x^2 - 5x + 0 = 0$	12) $1x^2 + 1x - 6 = 0$
13) $1x^2 - 6x + 5 = 0$	14) $2x^2 + 0x - 24 = 0$
15) $4x^2 - 4x + 1 = 0$	

Warning: Don't forget to check solutions to radical equations in the **original** equation.

Solutions:

1) $x = -7, 6$	2) $x = 1, 10$
3) $t = 2 \pm 2i$	4) $x = -1, 6$
5) $x \approx -1.10, 1.60$	6) $x = \frac{1}{2}, 2$
7) $x = -4, -\frac{2}{3}$	8) $x = -8, 7$
9) $x = \frac{5}{6}, -\frac{1}{3}$	10) $x = 2 \pm 7i$
11) $x = 5$ only	12) $x = 2$ only
13) $x = 5$ only	14) no solution
15) $x = \frac{1}{2}$	